

# A Neural Net-Based Approach for CPU Utilization

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**Abstract**— CPU scheduling is an important subject to maximize CPU utilization in the context of operating systems. Multiprogramming operating systems need CPU scheduling for organization of processes to be executed. The order of process execution is determined by a CPU scheduling policy in use. The utilization of CPU depends on the selection of scheduling algorithms. There are several scheduling policies in the literature such as First-Come, First-Served scheduling, Shortest-Job-First scheduling, Last-Come, First-Served scheduling, Priority scheduling. On the other hand, there are some criteria (waiting time, throughput number, turnaround time, response time) to measure the efficiency of these policies. It is important that we choose the scheduling policy which has the minimum waiting time as this is crucial stage of utilizing CPU efficiently. This paper explores an alternative, neural network approach to build a CPU scheduling model to obtain the waiting time measure. In this paper, we will show that neural networks can be used to model scheduling policies and can predict the waiting time of processes. Three learning algorithms and three different neuron numbers in the hidden layer of the network are studied to boost the efficiency of neural network model for waiting time prediction. A comparison between Neural-Network Based Model and First-Come, First-Served scheduling, Shortest-Job-First scheduling, Last-Come, First-Served scheduling are provided. The results reveal the effectiveness of neural networks in predicting waiting times, and thus suggest that it can be useful and practical addition to the framework of operating systems.

**Keywords**— CPU Scheduling, Operating Systems, Neural Networks.

## CPU Kullanımı için Yapay Sinir Ağı Tabanlı Yaklaşım

**Özet**— CPU kullanımını maksimize etmek için kullanılan CPU zamanlama, işletim sistemlerinde önemli bir konudur. Çoklu programlamalı işletim sistemleri, çalıştırılacak işlemlerin organize edilmesi için CPU zamanlamasına ihtiyaç duyarlar. Çalıştırılacak işlemlerin sırası kullanılan CPU zamanlama politikası tarafından belirlenir. CPU kullanımı seçilen zamanlama algoritmasına bağlıdır. Literatürde, İlk Gelen Önce zamanlama, En Kısa İş zamanlama, Son Gelen Önce zamanlama, Öncelikli zamanlama gibi farklı algoritmalar bulunmaktadır. Diğer yandan, bu zamanlama politikalarının verimliliğini ölçmek için kullanılan bazı kriterler (bekleme süresi, iş üretimi sayısı, dönüş süresi, yanıt süresi) vardır. Minimum bekleme süresine sahip zamanlama algoritmasının seçimi CPU kullanımının verimli olması açısından önemli bir aşamadır. Bu çalışma, yapay sinir ağı yaklaşımının CPU zamanlama modeli oluşturarak bekleme süresi ölçütünü elde etmede kullanılabilirliğini araştırmaktadır. Bu çalışma ile yapay sinir ağlarının zamanlama politikalarının modellenmesinde kullanılabileceği ve işlemlerin bekleme zamanını tahmin edebileceği gösterilecektir. Yapay sinir ağı modelinin bekleme süresi tahmini için verimliliğini artırmak amacı ile üç farklı öğrenme algoritması ve her öğrenme algoritması için üç farklı gizli katman nöron sayısı çalışılmıştır. Yapay sinir ağı tabanlı model ile İlk gelen önce zamanlama, En kısa iş zamanlama, Son gelen önce zamanlama algoritmalarının karşılaştırılması sağlanmaktadır. Sonuçlar yapay sinir ağı yaklaşımının bekleme süresi tahminindeki etkinliğini göstermektedir ve böylece işletim sistemleri çerçevesine faydalı ve pratik bir katkı sağlanmaktadır.

**Anahtar Kelimeler**— CPU Zamanlama, İşletim Sistemleri, Yapay Sinir Ağları.

### 1. INTRODUCTION

Scheduling is the way of sharing computer resources between multiple processes by operating system. Operating system switches CPU among the processes according to a scheduling policy in use [1].

One of the purposes of the operating system is keeping CPU as busy as possible to maximize the performance of

the CPU and to make the computer more productive. The objective is to have some process running at all times, to maximize CPU utilization. Because, maximizing CPU utilization means maximizing the overall performance of the computer system. Therefore, CPU scheduling is considered as a fundamental topic in operating system concept. Since the execution order of processes is determined by scheduling policies, CPU utilization depends on the selection of the scheduling policy to be

used. There are several scheduling policies in the literature such as First-Come, First-Served policy, Shortest-Job-First policy, Last-Come, First-Served policy, Priority policy. Scheduling policies are generally classified into preemptive and non-preemptive scheduling disciplines[1-3].

**Preemptive Scheduling** : running task may be interrupted for some time and resumed later when the priority task has finished its execution.

**Non-preemptive Scheduling** : running task is executed without interruption. It cannot be interrupted until terminated.

The choice of a particular policy may favor one class of processes over another. In choosing which policy to use in a particular situation, we must consider the algorithmic properties of these policies. There are several criteria to measure the efficiency of these algorithms [2] :

1. *CPU utilization* : It is defined as the value of time CPU is in use. The goal of the CPU scheduling is to maximize the CPU utilization.

2. *Throughput* : It is defined as the number of processes that are completed per time unit.

3. *Turnaround Time* : It is defined as a total time which is spend to complete the process from the time of submission to the time of completion.

4. *Response Time* : It is defined as the time passed until the first response is produced for a process execution.

5. *Waiting Time* : It is defined as the total time a process has been waiting in ready queue.

6. *Context Switch* : It is defined as a computing process of storing and restoring state of a CPU so that execution can be resumed from same point at a later time. Context switch are usually computationally intensive, lead to wastage of time, memory, scheduler overhead so much of the design of operating system is to optimize these switches.

The goal of the CPU scheduling is to maximize CPU utilization and throughput and to minimize turnaround time, waiting time, and response time. Therefore, minimum waiting time is one of the characteristics of the effective scheduling algorithm.

Recently, a great deal of papers have conducted important resercahes into the CPU scheduling algorithms and their performances. In [3], a new CPU scheduling algorithm called MIN-MAX has been proposed, focusing on the comparative study of the existing algorithms on the basis of various scheduling parameters with the proposed algorithm MIN-MAX. In [4]-[6], the review of different

scheduling algorithms has been performed with different parameters, such as running time, burst time and waiting times etc. The CPU scheduling algorithm with improved performance has been presented in [7]. The technique used in this paper for increasing the speed up factor is 'Pipelining'. This technique can be applied to any CPU scheduling algorithm to improve its performance. [8] has carried out a comparative study of various scheduling algorithms for a single CPU and determines which algorithm may be the best for a specific situation. [9] has proposed a new CPU scheduling algorithm called Combinatory that combines the functions of some basic scheduling algorithms. In [10], the author has developed an interactive Java-based simulator that uses graphical animation to convey the concepts of various CPU scheduling algorithms. A CPU scheduling algorithm that can handle all types of processes with optimum scheduling criteria has been proposed in [11]. In [12], a new Round Robin scheduling algorithm has been given. The authors of [13] have realised the implementation of a new CPU scheduling algorithm called An Optimum Multilevel Dynamic Round Robin Scheduling (OMDRRS) in order to improve Round Robin scheduling algorithm using dynamic time slice concept. They have also simulated the behavior of various CPU scheduling algorithms. The authors of [14] have simulated different scheduling algorithms and evaluated their performances (throughput, latency, utilization, turnaround time, and waiting time) in a multi-processor environment.

Neural networks have the ability to model a function without knowing the exact character of this function. Therefore, a neural network can be considered as a black box that needs to be well-defined for the problem interested. Unlike the traditional methods, in neural networks, the only thing we need is to determine the endpoints (inputs and outputs). Therefore, neural network models do not need to derive metrics from some certain types of equations. Since selecting a scheduling algorithm according to a minimum waiting time is a fundamental step to utilize CPU efficiently, it is important to determine whether a neural network could be used as a tool to generate waiting time. The aim of this paper is to evaluate neural networks as a computational tool to estimate the waiting time of process sets. Hence, we first establish neural networks as a method for modeling scheduling policies by showing that we can model three widely accepted policies; First Come-First Served (FCFS) scheduling policy, Last-Come, First-Served (LCFS) scheduling policy and Shortest-Job-First (SJF) scheduling policy. We use three different training algorithms and three different neuron numbers in the hidden layer of the network to evaluate the estimation results according to the network architecture and training method. The results of FCFS, LCFS and SJF scheduling algorithms and the designed neural network model are compared to show the effectiveness of the proposed method. Obtained results show that the estimation ability of designed neural network model is highly powerful. We also showed that the neural network approach can be considered as a

successful alternative method to calculate waiting time of processes to analyze CPU utilization when compared with the traditional methods.

## 2. SCHEDULING POLICIES

Scheduling policies decide which of the processes in the ready queue is to be allocated the CPU. In this study, we considered the following scheduling policies that all are non-preemptive scheduling algorithms to calculate the waiting time criterion and to train the designed neural network according to these results.

### 2.1 First-Come, First-Served Scheduling

FCFS, allows a process that requests CPU first, holds the CPU first. Process in ready queue is executed on the basis of arrival time, without any preemption. Once CPU has started executing a process, it cannot be interrupted unless completed.

### 2.2 Last-Come, First-Served Scheduling

LCFS, allows a process that requests CPU last, holds the CPU first. The last process in ready queue is executed without any preemption.

### 2.3 Shortest-Job-First Scheduling

Burst time is exact time that is required to complete execution of particular process. CPU scheduling algorithms require burst time as input. SJF, allows a process with the minimum burst time holds the CPU first. FCFS policy is used, when two processes have the equal CPU burst time.

## 3. NEURAL NETWORKS

Neural networks are powerful mathematical and computational tools widely used for estimating engineering problems due to their ability of learning. In recent years, neural network systems have become a popular solving technique and are used in many fields such as accounting, civil engineering, mine engineering, environmental engineering, medicine, etc. Designing an appropriate neural network model for the system in interest is a fundamental issue in neural network approach [15-19]. Therefore, designing an estimating model for CPU scheduling by Neural Networks can be considered as a significant concept in both operating systems and neural networks fields. Since selecting a scheduling algorithm according to a minimum waiting time is a crucial step to utilize CPU efficiently, it can be considered as an intuitive decision making method to design a neural network model to estimate total waiting time of processes.

A typical feed-forward neural network model consists of three layers of neurons that are input, hidden, and output. When a feed-forward neural network is being trained, the connection weights are updated to minimize the error between the desired and estimated values of the system variables [20].

In this study, we have designed a feed-forward neural network with one hidden layer to estimate waiting time of

processes in Table 1. Three distinct training algorithms (Levenberg - Marquardt (L-M) Algorithm, Conjugate - Gradient (C-G) Algorithm with Polak-Ribiere updates, Gradient - Descent (G-D) Algorithm) are used to train the network [21-25]. The number of hidden neurons is chosen to be 10, 20 and 30 for each algorithm to evaluate the optimum result of the network. Input layer consists of 10 nodes, and an output layer consists of 1 node. The inputs are the burst times for 10 processes, shown in Table 1, that are randomly generated. The output is the estimated waiting time value.

Mathematically, a hidden or output unit operates as follows :

$$y_j = f \left( \sum_i w_{ji} x_i + b_j \right), i = 1, 2, \dots, m, j = 1, 2, \dots, n \quad (1)$$

where  $m$  is the number of the inputs,  $n$  is the number of the outputs,  $y_j$  is transformed output by the  $j$  th hidden or output node,  $f$  is an activation function,  $w_{ji}$  is the synaptic weight from the  $i$ th node to  $j$ th node,  $x_i$  is an input node,  $b_j$  is bias at  $j$ th node.

50 column input vectors are used with the dimension (10x1), and 50 outputs are derived as a scalar value. In MATLAB simulation of this case study, inputs are given as a matrix of size (50x10) and the output is obtained as (50x1) column vector for 50 queues of 10 processes.

$$\begin{aligned} x_p &= [x_1, x_2, \dots, x_{10}]^T, & p &= 1, 2, \dots, 50 \\ w &= [w_1, w_2, \dots, w_{10}]^T \\ y_p &= f(w_i x_i) = f(w^T x), & p &= 1, 2, \dots, 50 \end{aligned} \quad (2)$$

where  $p$  is a set number of 10 processes given in Table 1., components of input vector,  $x_p$ , are burst times of processes for  $p$ th set and an output  $y_p$  is a waiting time for the  $p$ th set.

## 4. PROPOSED WORK

In this study, we randomly generated burst times for 10 processes as given in Table 1 since there is not a database including real burst time values. On the other hand, this situation does not effect the accuracy of the results of the proposed network because once we train the network it will work for every value. Then, we used these values to find the waiting time of each set according to FCFS, LCFS and SJF policies as given in Table 2. These obtained results are used to train the designed network model under three different training algorithms (Levenberg - Marquardt Algorithm, Conjugate - Gradient Algorithm with Polak-Ribiere updates and Gradient - Descent Algorithm) as 70% for training, 15% for validation, and 15% for testing. The node number in hidden layer is applied as three different values (10, 20 and 30) for each training algorithm to see the optimum result. Hence, 9 different estimated results are calculated for each scheduling policy. The block diagram of the proposed system is given in Figure 1. Table 3 shows the

estimated results of 9 distinct neural network model for FCFS policy for each set. Table 4 shows the estimated results of 9 distinct neural network model for LCFS policy. Table 5 shows the estimated results of 9 distinct neural network model for SJF policy.

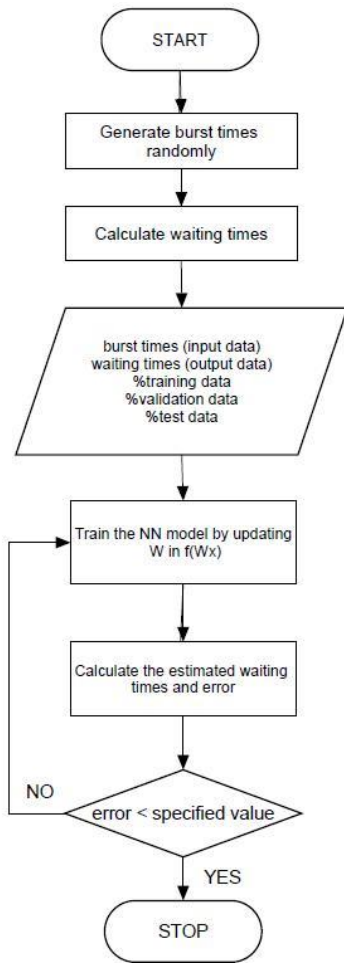


Figure 1. The block diagram of the proposed system

5. RESULTS AND ANALYSIS

We analyzed three different CPU scheduling algorithm by intending to design a proper neural network model. Hence, we used three different training algorithms and the neuron number of the hidden layer of the network is taken into account for three different values to see the optimum results of the neural network model. Therefore, we get 9 results for each scheduling policy and 27 results totally. Table 6. shows the average difference values of the results of the scheduling policies and the designed neural network for process sets.

Table 1. Burst Times of processes for 50 Different Process Set

PROCESS SET	P1	P2	P3	P4	P5	P6	P7	P8	P9	P10
1	6	8	17	4	22	5	24	19	37	20

2	11	7	26	30	32	15	9	10	16	8
3	9	11	17	18	24	46	12	14	28	10
4	42	47	16	52	38	14	22	21	16	36
5	85	32	43	50	17	18	21	7	12	24
6	12	14	28	10	37	60	64	12	35	10
7	22	21	16	36	25	5	12	22	5	24
8	21	7	12	24	13	44	35	32	15	9
9	18	19	20	24	36	38	45	22	21	55
10	12	38	14	22	21	32	33	90	77	54
11	25	17	18	21	58	38	42	41	82	37
12	34	37	60	64	65	24	76	55	37	19
13	8	25	5	12	17	42	34	85	24	23
14	11	13	44	35	48	16	32	48	64	11
15	14	9	22	95	37	48	14	42	75	33
16	26	45	53	14	33	16	36	80	8	17
17	98	12	52	54	36	12	24	49	48	59
18	5	82	89	37	71	35	10	42	25	80
19	46	11	12	55	42	5	24	15	62	41
20	34	25	32	35	37	14	22	5	20	6
21	76	28	74	52	9	41	32	15	8	11
22	77	75	88	90	51	40	24	46	10	9
23	90	37	20	68	87	39	38	14	36	42
24	88	42	23	37	85	62	17	18	24	85
25	15	90	84	61	51	40	37	60	10	12
26	25	96	16	36	42	84	25	5	24	18
27	26	14	12	24	17	55	13	44	60	27
28	28	34	35	10	24	26	36	38	50	35
29	32	55	5	24	38	61	21	32	34	65
30	45	52	64	84	31	42	56	77	41	20
31	48	17	9	24	28	39	45	51	11	80
32	91	14	42	37	42	22	24	41	14	52
33	84	18	85	85	49	21	25	18	26	65
34	65	60	12	64	57	7	64	46	98	80
35	12	5	18	19	77	19	38	14	5	25
36	26	44	27	28	64	38	36	18	46	13
37	36	38	35	39	60	17	25	60	34	9
38	5	32	21	7	97	94	26	55	76	45
39	22	38	22	34	45	27	19	84	77	12
40	27	19	20	21	48	24	64	55	90	82
41	91	10	25	5	37	9	9	26	88	11
42	45	9	26	44	33	18	42	61	15	16
43	65	51	36	38	36	52	85	30	7	12
44	37	87	21	32	71	22	12	64	11	15
45	56	85	9	77	42	24	84	78	47	36
46	78	51	42	51	37	98	66	41	32	40
47	87	42	10	24	26	36	38	50	14	11
48	34	17	24	38	61	21	32	34	65	24
49	16	42	23	37	38	61	21	75	39	50
50	99	90	51	40	24	46	10	9	28	37

**Remark 1.** This case study is applied for 50 process sets including 10 processes whose burst times are randomly generated. It should be noted that, the proposed model can be applied to process set of any length.

**Remark 2.** In this case study, 9 different neural network models are designed to analyze the results of the network for each scheduling policy. Among these models, the best solution is obtained by the network with 10 hidden nodes under L-M algorithm for FCFS policy. The best solution for LCFS policy is obtained by the network with 10 hidden nodes under G-D algorithm. The best solution for SJF policy is obtained by the network with 10 hidden nodes under L-M algorithm. The regression graphics of these network models are given by Figure 3, Figure 3, and Figure 4, respectively. The regression values are obtained to be very close to 1 which is a desired case for modeling by NNs.

Table 2. Waiting Times of Process Sets Under FCFS, LCFS, SJF Scheduling Policies

PROCESS SET	WAITING TIME UNDER FCFS	WAITING TIME UNDER LCFS	WAITING TIME UNDER SJF
1	538	920	455
2	800	676	495
3	792	909	578
4	1548	1188	991
5	1868	913	819
6	1152	1386	747
7	924	768	597
8	898	1010	627
9	1130	1552	1015
10	1231	2306	1090
11	1345	2066	1197
12	2202	2037	1601
13	928	1547	691
14	1281	1617	950
15	1500	2001	1033
16	1554	1398	911
17	2112	1884	1347
18	2180	2104	1357
19	1310	1507	864
20	1277	793	720
21	2081	1033	880
22	3038	1552	1470
23	2423	1816	1455
24	2295	2034	1396
25	2465	1675	1303
26	1976	1363	944
27	1066	1562	860
28	1287	1557	1157
29	1502	1801	1154
30	2459	2149	1773
31	1319	1849	1010
32	1913	1498	1147
33	2471	1813	1377
34	2228	2749	1781
35	996	1092	564
36	1605	1455	1137
37	1704	1473	1167
38	1615	2507	1155
39	1495	1925	1098
40	1389	2661	1324
41	1492	1307	635
42	1423	1358	942
43	2183	1525	1239
44	1986	1362	974
45	2470	2372	1707
46	2599	2225	1887
47	1835	1207	942
48	1456	1694	1168
49	1549	2069	1328
50	2588	1318	1172

**Remark 3.** The optimum results of the neural network models are obtained when the number of processes and the number of hidden nodes are equal.

**Remark 4.** The minimum waiting time is provided by SJF policy for each process set and the results of the designed neural network model show the same tendency.

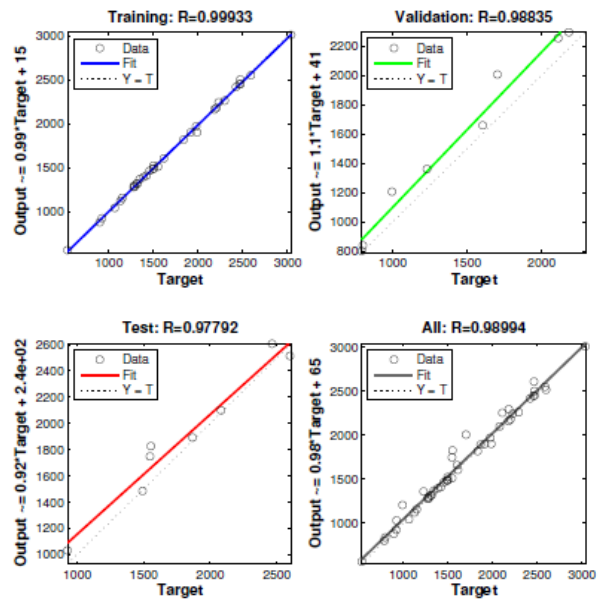


Figure 2. The regression coefficients of NN model with 10 hidden nodes under L-M Alg. For FCFS policy

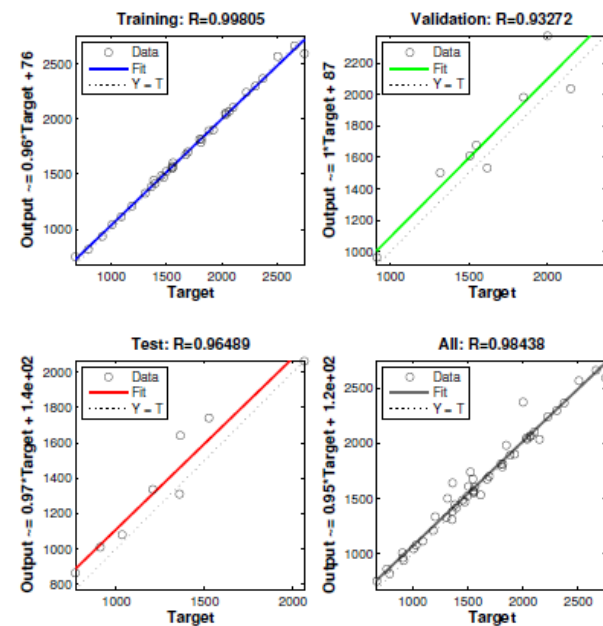


Figure 3. The regression coefficients of NN model with 10 hidden nodes under G-D Alg. For LCFS policy

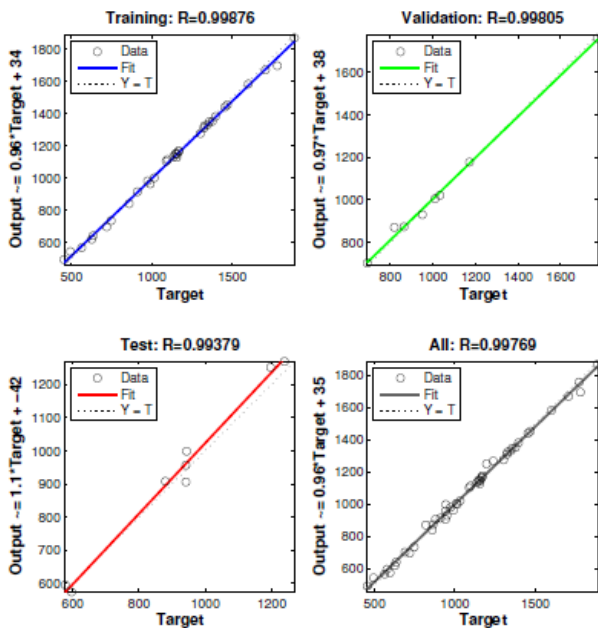


Figure 4. The regression coefficients of NN model with 10 hidden nodes under L-M Alg. For SJF policy

## 6. CONCLUSIONS

Minimum waiting time is one of the characteristics of efficient CPU scheduling policies. Selecting an appropriate scheduling policy according to a minimum waiting time is a fundamental step to utilize CPU efficiently. The aim of this paper is to explore a neural network approach to build a CPU scheduling model to generate waiting time. This study establishes neural networks as a method for modeling scheduling policies by showing that we can model three widely accepted policies; First Come-First Served (FCFS) scheduling policy, Last-Come, First-Served (LCFS) scheduling policy and Shortest-Job-First (SJF) scheduling policy. For this purpose, different training algorithms and various number of hidden neurons are applied in the process of designing neural network model. The optimum results have been acquired when the number of processes and hidden neurons are equal. In our proposed neural network system, the training results have shown that the L-M algorithm best fits for FCFS and SJF policies, and G-D training algorithm best fits for LCFS policy. The proposed model can be applied to the process set of any length. This paper proved that applying neural network approach to CPU utilization can be an alternative successful method to obtain waiting time criterion.

## REFERENCES

- [1] A. Silberschatz, P. B. Galvin, G. Gagne, **Operating System Concepts, Sixth Edition**, John Wiley and Sons Inc., New York, A.B.D., 2004.
- [2] M. Milenkovic, **Operating Systems Concepts and Design, Second Edition**, McGraw-Hill, Computer Science Series, 2010.

- [3] K. Sukhija, N. Aggarwal, M. Jindal, "An Optimized Approach to CPU Scheduling Algorithm:Min-Max", *Journal Of Emerging Technologies inWeb Intelligence*, 6, 420-428, 2014.
- [4] M. Saini, N. Kumar, "A Survey on CPU Scheduling", *International Journal Of Research In Computer Applications and Robotics*, 3, 7-12, 2015.
- [5] S.Jain and S.Jain, "A Review study on the CPU Scheduling Algorithms", *International Journal of Advanced Research in Computer and Communication Engineering*, 5, no.8, 2016.
- [6] Imran Qureshi, "CPU Scheduling Algorithms: A Survey", *Int. J. Advanced Networking and Applications*, 5, no.4, 1968-1973, 2014.
- [7] H. Arora, D. Arora, B.Goel, P. Jain, "An Improved CPU Scheduling Algorithm", *International Journal of Applied Information Systems*, 6, 7-9, 2013.
- [8] N. Goel, R.B. Garg, "A Comparative Study of CPU Scheduling Algorithms", *International Journal of Graphics and Image Processing*, 2, 245-251, 2012.
- [9] S. Bibi, F. Azam, Y. Chaudhry, "Combinatory CPU Scheduling Algorithm", *International Journal of Computer Science and Information Security*,8, 39-43, 2010.
- [10] S. Suranauwarat, "The Design and Development of a CPU Scheduling Algorithm Simulator", *In Proc. of 12th WSEAS International Conference on Applied Computer Science*, 164-170, 2012.
- [11] M. Sindhu, R. Rajkamal, P. Vigneshwaran, "An Optimum Multilevel CPU Scheduling Algorithm", *International Conference on Advances in Computer Engineering*, 90-94, 2010.
- [12] Raman, P.K.Mittal, "An Efficient Dynamic Round Robin CPU Scheduling Algorithm", *International Journal of Advanced Research in Computer Science and Software Engineering*, vol.4, no.5, 2014.
- [13] N.Goel, R.B.Garg, "Simulation of an Optimum Multilevel Dynamic Round Robin Scheduling Algorithm", *International Journal of Computer Applications*, 76, 7, 42-46, 2013.
- [14] S. Almakdi, M. Aleisa, M. Alshehri, "Simulation and Performance Evaluation of CPU Scheduling Algorithms", *International Journal of Advanced Research in Computer and Communication Engineering*, 4, 2015.
- [15] S. Yang, D. Wang, T. Chai, G. Kendall, "An improved constraint satisfaction adaptive neural network for job-shop scheduling", *Journal of Scheduling*, 13, 17-38, 2010.
- [16] M.D. Richard, R.P. Lippmann, "Neural Network Classifiers Estimate Bayesian a posteriori Probabilities", *Neural Computation*, 3, 461-483, 1991.
- [17] A.A. Collister, O. Lahav, "ANNz: Estimating Photometric Redshifts Using Artificial Neural Networks", *Publications of the Astronomical Society of the Pacific*, 116, 345-351, 2004.
- [18] M. Kumar, N. S. Raghuvanshi, R. Singh, W. Wallender, W. Pruitt, "Estimating Evapotranspiration using Artificial Neural Network", *Journal of Irrigation And Drainage Engineering*, 128, 224-233, 2002.
- [19] M. Uzunoglu, C. Kocatepe, R. Yumurtaci, "An Artificial Neural Network Based Preestimation Filter For Bad Data Detection Identification and Elimination In State Estimation", *Mathematical and Computational Applications*, 1, 159-164, 1996.

[20] S. Haykin, **Neural Networks and Learning Machines (3rd Edition)**, Prentice Hall., 2009.

[21] K. Levenberg, "A method for the solution of certain problems in least squares", *Quarterly of Applied Mathematics*, 5, 164-168, 1944.

[22] D. Marquardt, "An algorithm for least-squares estimation of nonlinear parameters", *SIAM Journal on Applied Mathematics*, 11, 431-441, 1963.

[23] H. Yuand, B. M. Wilamowski, **Intelligent Systems, Chapter 12, LevenbergMarquard Training**, CRC Press., 2011.

[24] M. Hestenes, E. Stiefel, "Methods of Conjugate Gradients for Solving Linear Systems", *Journal of Research of the National Bureau of Standards*, 49, 409-436, 1952.

[25] M. Avriel, **Nonlinear Programming: Analysis and Methods**, Dover Publishing., 2003.

Table 3. All Results of 9 NN model for FCFS Policy

Process Set	10-Node L-M Alg.	20-Node L-M Alg.	30-Node L-M Alg.	10-Node C-G Alg.	20-Node C-G Alg.	30-Node C-G Alg.	10-Node G-D Alg.	20-Node G-D Alg.	30-Node G-D Alg.
1	563.3358	515.7816	847.3712	590.5264	893.4663	538.0000	537.1191	628.6688	538.0000
2	838.3434	768.6529	1196.8678	820.7253	800.0000	800.0000	799.4765	875.6751	800.0000
3	801.1347	760.7168	790.3533	826.3715	792.0000	792.0000	859.8623	604.8718	792.0000
4	1648.1870	1533.8790	1547.0681	1565.7740	1548.0000	1548.0000	1546.6650	1564.9830	1548.0000
5	1891.7890	1849.8259	1867.5340	1931.4770	1868.0000	1170.6650	2038.5440	1615.4410	1868.0000
6	1158.0150	1129.4895	1773.8321	1191.9850	1579.6980	1343.3420	1151.4450	1188.9230	1380.3650
7	925.8820	900.5603	1552.5876	967.9123	945.5376	696.6961	912.6073	1100.5910	866.6014
8	878.7025	868.1511	894.6057	936.6642	898.0000	898.0000	896.8202	967.0436	845.9406
9	1122.4230	1115.0268	1128.2988	1143.2050	1285.4900	1130.0000	1229.3670	955.0412	1130.0000
10	1350.1810	1228.8870	1230.2027	1267.4680	1231.0000	1231.0000	1231.2750	886.9156	1653.1440
11	1369.5910	1332.8506	1344.3096	1353.6780	1345.0000	1345.0000	1301.6430	1367.3590	1345.0000
12	2178.9060	2188.1394	2201.9207	2224.1190	2386.4820	2390.1720	2200.7600	2216.2720	2202.0000
13	1030.9370	924.7103	925.7904	1016.1730	997.0957	928.0000	982.5115	986.9197	928.0000
14	1294.7680	1272.3975	1279.9523	1315.7240	1281.0000	1281.0000	1218.0370	1146.3340	1281.0000
15	1523.5930	1525.6027	1499.4663	1495.3830	1524.2570	1500.0000	1395.9510	1139.2190	1500.0000
16	1706.7700	1546.1120	2155.9733	1688.6860	1425.2770	2747.7540	1553.0010	1587.1460	1554.0000
17	2253.7120	2101.4670	1571.4588	2245.8990	2112.0000	2112.0000	2111.2510	2118.7970	2112.0000
18	2160.2430	2148.2474	2180.0743	2163.1520	3429.5310	1445.4230	2579.0410	2186.7520	2180.0000
19	1318.0530	1297.8887	726.5543	1316.5360	1310.0000	1310.0000	1322.0800	1320.4350	1310.0000
20	1278.9840	1179.7643	1274.8862	1317.6240	1272.5610	1277.0000	1276.3260	1308.6990	1277.0000
21	2099.7710	2063.4917	1427.3614	2002.4420	2081.8180	2669.8810	2194.7050	2067.7820	2217.4310
22	3008.0080	2764.0809	2795.8841	2758.3790	3038.0000	3038.0000	3037.6430	3008.8620	2272.7320
23	2417.6530	2420.0576	1668.5868	2281.8380	2423.0000	2423.0000	2422.7030	2435.9260	2336.6040
24	2260.8330	2176.5101	2294.7961	2263.1910	2640.2400	2295.0000	2394.6240	2705.3370	2295.0000
25	2607.5340	2530.3026	2267.3111	2474.3310	2526.4860	2465.0000	2464.1680	2380.6760	2803.5360
26	1970.4360	1983.5091	1975.7587	1970.9870	1976.0000	1976.0000	2011.2540	1974.5730	1976.0000
27	1042.8250	1056.4903	1063.6889	1119.7340	1066.0000	883.2344	1065.5960	1009.4500	1066.0000
28	1281.0590	1310.6423	1285.3303	1410.6940	1287.0000	1658.4120	1286.7280	1315.6350	1287.0000
29	1488.5740	1378.8923	1519.2737	1517.4670	1502.0000	2064.3360	1582.5690	2031.2370	1502.0000
30	2447.4670	2447.5120	2458.7987	2451.8590	2459.0000	2459.0000	2269.1700	2230.5780	2459.0000
31	1317.3540	1321.3305	1319.4513	1311.5290	1463.7700	1319.0000	1278.6230	1336.2790	1319.0000
32	1898.9960	1904.0010	1912.5567	1916.0770	1913.0000	1913.0000	1912.6100	1916.2410	1240.8950
33	2449.3060	2703.5959	2470.6856	2362.3550	2471.0000	2471.0000	2470.8260	1945.8580	2471.0000
34	2243.6540	2036.2273	2207.9979	2172.0220	2228.0000	2228.0000	2287.2310	2223.3210	2228.0000
35	1006.2010	992.1551	2200.5614	915.8697	996.0000	996.0000	996.1771	1050.6350	1239.6700
36	1658.4790	1592.5319	1604.2166	1622.9930	1605.0000	1781.7750	1603.9660	1630.2560	1605.0000
37	1786.0190	1699.0770	1703.1819	1770.9780	1704.0000	1704.0000	1703.2680	1828.3580	1441.1900
38	1605.3800	1612.8619	1615.4448	1640.1610	1615.0000	1615.0000	1632.2480	1629.0180	2390.8330
39	1488.8620	1390.4569	1494.0077	1524.7790	1495.0000	1495.0000	1494.4050	1548.7000	935.7278
40	1394.1040	1381.1707	1389.3388	1431.3240	1389.0000	1389.0000	1389.3830	1406.1870	1905.4430
41	1484.6870	1503.7724	1162.6850	2105.3590	1492.0000	1353.1930	1491.9060	1503.2430	1492.0000
42	1410.5000	1390.8623	1422.7309	1494.7570	1423.0000	1423.0000	1314.8920	1469.1090	1469.1090
43	2293.8210	2158.3797	2183.7101	2179.7600	2183.0000	2183.0000	2236.0400	3195.1270	3195.1270
44	1900.8330	1894.1307	1985.6707	1795.9260	2442.7040	2797.4250	1985.7230	2001.3150	2001.3150
45	2500.8090	2228.6573	2469.7746	2474.2020	2470.0000	2470.0000	2469.2640	2427.5200	2427.5200
46	2515.0930	2358.3229	2599.1299	2504.9000	2754.5030	2682.0910	2599.4560	2580.8710	2580.8710
47	1818.2540	1820.8530	1836.4277	1963.4790	1835.0000	2757.6190	1705.9680	1844.4360	1844.4360
48	1463.6340	1452.8767	1467.5955	1472.1140	1456.0000	1456.0000	1455.2030	1479.1040	1479.1040
49	1512.3280	1559.6771	1567.9290	1568.0700	1549.0000	1549.0000	1549.0750	1578.7470	1578.7470
50	2549.8920	2584.8221	2587.7862	2529.7380	2588.0000	2110.0730	2698.6620	2564.8170	2564.8170

Table 4. All Results of 9 NN model for LCFS Policy

Process Set	10-Node L-M Alg.	20-Node L-M Alg.	30-Node L-M Alg.	10-Node C-G Alg.	20-Node C-G Alg.	30-Node C-G Alg.	10-Node G-D Alg.	20-Node G-D Alg.	30-Node G-D Alg.
1	937.8915	920.0000	944.2013	950.5981	898.0092	938.0062	929.3108	920.1202	920.0000
2	722.6814	676.0000	743.7531	675.9177	664.2900	849.0036	675.8433	579.6319	676.0000
3	990.7845	1087.1640	944.5030	908.9595	898.3317	909.0000	899.9115	909.1029	909.0000
4	1210.9230	1264.9470	900.4425	1117.82	1204.0420	1188.0000	1187.9820	1188.0780	1188.0000
5	962.9023	739.9513	536.2939	1094.82	921.5349	1072.4360	953.0079	1180.0810	913.0000
6	1444.7580	1386.0000	1278.7950	1385.642	1703.3030	1386.0000	1512.6050	1357.7190	1386.0000
7	842.8548	768.0000	677.4106	767.9866	700.1255	768.0000	767.9472	768.0173	768.0000
8	1044.1680	1010.0000	760.0232	1010.002	773.7024	1010.0000	1009.9980	1010.2100	1010.0000
9	1551.4660	1433.3660	1398.7040	1552.008	1547.9830	1552.0000	1551.9940	1552.0500	1552.0000
10	2295.6850	2350.7070	2429.8920	2305.917	2598.1290	2306.0000	2406.0000	1839.9190	1893.0530
11	2062.1480	2078.8760	1870.3700	2065.873	2044.4240	2066.0000	2065.9890	2066.0290	2066.0000
12	2037.1910	2037.0000	2122.0230	2036.954	2026.6050	2037.0000	2037.0000	2348.5980	2015.3250
13	1676.3520	1547.0000	1521.0950	1776.283	1506.1980	1547.0000	1367.0580	1547.1480	1558.1000
14	1532.3060	1617.0000	1388.9390	1616.763	1576.1500	1617.0000	1616.9290	1759.7290	1617.0000
15	2171.8190	2001.0000	2211.7090	2000.955	1993.4600	2001.0000	2000.9470	2000.8090	2772.3960
16	1415.3150	1398.0000	1441.7780	1397.835	1381.3420	1961.7670	1297.9090	1416.5160	1404.1750
17	1891.3920	1884.0000	1716.5550	1883.963	1881.9550	1842.7660	1883.9920	2183.6230	1715.1370
18	2103.3050	2104.0000	2149.6300	2103.985	2097.0860	2104.0000	2094.1170	2103.9820	2104.0000
19	1609.5160	1507.0000	958.6304	1506.84	1508.4670	1507.0000	1506.9660	1506.8430	1507.0000
20	818.0318	793.0000	717.0918	792.9026	795.0093	793.0000	792.9388	747.3302	793.5628
21	1078.5070	1033.0000	944.8952	1032.889	1142.4810	1033.0000	1033.0240	1033.0540	1033.0000
22	1572.1660	1552.0000	1836.7400	1560.042	1606.6980	302.1984	1552.0490	1551.9760	1552.0000
23	1811.9360	1799.3860	1568.7750	1815.932	1941.8410	1454.0360	2171.6100	1815.8970	1397.8940
24	2049.8840	2331.4780	1694.7330	2022.578	2057.8220	2034.0000	2176.5210	2034.0950	2199.5180
25	1675.4540	1887.0800	844.0410	1767.331	1532.7340	1675.0000	1886.9170	2124.8730	1675.0000
26	1440.8450	1363.0000	1238.3680	1362.981	1382.5280	1363.0000	1362.9120	1363.0130	1363.0000
27	1602.9220	1562.0000	1424.7830	1561.713	1521.4210	1537.8680	1663.0000	1562.0930	1922.9870
28	1560.1090	1557.0000	1491.3380	1556.757	1542.1900	1711.9570	1556.9740	1557.1350	1700.2240
29	1813.8380	1801.0000	1677.2940	1801.04	1797.7610	1801.0000	1801.0090	1851.1360	2226.5680
30	2035.8580	1549.2360	2621.0260	2215.179	2148.2770	2149.0000	2148.9830	2148.8380	2149.0000
31	1981.7090	1849.0000	2573.1440	1848.999	1867.3540	1849.0000	1849.0000	1849.6600	1849.0000
32	1522.4950	1359.0160	1672.6750	1497.876	1472.0990	1498.0000	1498.0080	1849.1440	1160.1360
33	1786.4390	1602.9220	2038.0500	1812.931	1796.0060	1909.4460	1804.0900	2028.3540	1813.0000
34	2590.6770	2608.7580	2218.4120	2749.078	2748.4050	2749.0000	2657.9810	2748.9560	2005.1340
35	1114.8430	1092.0000	873.7934	1477.199	900.7235	889.4609	1091.9250	1091.9560	1092.0000
36	1485.6260	1455.0000	1556.8000	1583.272	1433.3610	1455.0000	1454.9650	1455.0620	1455.0000
37	1469.2550	1473.0000	1369.7700	1472.849	1663.2250	1607.8880	1472.9790	1472.9020	1308.3270
38	2565.1590	2507.0000	1961.9090	2506.871	2047.9320	2507.0000	2506.9630	2507.0040	2507.0000
39	1900.7610	1775.3960	2027.1120	1861.454	2225.8970	1925.0000	1922.4980	1924.9950	1925.0000
40	2660.6400	2670.0000	2059.4970	2661.005	2913.6340	2661.0000	2661.0120	2661.0230	2661.0000
41	1327.0480	1387.4500	589.2895	1520.68	1304.6320	1334.3590	1406.9810	1307.2010	1307.0000
42	1309.4590	1358.0000	1142.3020	1447.833	1343.8010	1238.6680	1358.0140	1357.8780	1358.0000
43	1670.4200	1525.0000	1187.8210	1363.776	1417.5630	1525.0000	1722.8320	1524.8760	1525.0000
44	1383.6860	1362.0000	1286.7210	1362.004	1368.9350	1477.4980	1609.4050	1362.1000	1362.0000
45	2364.0810	2372.0000	2274.6680	2372.053	2367.2710	2372.0000	2342.2400	2371.8970	2372.0000
46	2239.4360	2225.0000	2876.7390	2224.981	2268.8140	2225.0000	2224.9670	2224.9450	2225.0000
47	1335.3340	1207.0000	724.4970	1294.51	1000.1670	1128.3140	1382.2970	1206.9940	1207.0000
48	1700.3970	1790.3340	1460.1070	1693.817	1666.1420	1694.0000	1693.9620	1679.5140	1694.0000
49	2067.8170	2069.0000	2028.4030	2023.585	2026.8470	2069.0000	2068.9820	2068.9630	2069.0000
50	1431.4620	1361.7520	1338.2990	1317.997	1319.1560	1318.0000	1242.8950	1671.1680	1286.2100



Table 5. All Results of 9 NN model for SJF Policy

Process Set	10-Node L-M Alg.	20-Node L-M Alg.	30-Node L-M Alg.	10-Node C-G Alg.	20-Node C-G Alg.	30-Node C-G Alg.	10-Node G-D Alg.	20-Node G-D Alg.	30-Node G-D Alg.
1	492.5537	411.4987	421.9262	562.9937	698.1689	481.7583	481.7583	554.9838	571.0441
2	543.1882	432.4990	508.3105	499.0482	620.3964	615.5979	515.5979	505.4336	561.4124
3	595.9677	497.4110	697.4678	573.6829	680.8813	588.5218	588.5218	597.9939	639.4268
4	962.7445	1011.0640	817.8590	989.8972	989.6485	767.2904	810.8669	1390.9930	1067.1930
5	871.2825	785.8293	863.5327	817.0076	817.2058	833.1024	734.8605	918.9908	925.1859
6	734.2130	675.4574	747.7734	668.5055	594.8056	659.9185	677.6117	700.9942	839.1765
7	574.4386	551.1917	605.5168	695.5730	537.6758	608.9937	612.8375	696.9850	738.0142
8	619.1873	553.7844	632.7223	621.5709	622.6311	644.8910	709.1861	696.9909	706.3515
9	1000.4630	961.8336	1183.2620	1000.5890	1013.9910	1003.2740	1011.6100	1114.9920	1043.9230
10	1103.1790	1087.3310	1098.2900	1068.6240	1088.6700	1096.8530	1195.3300	1189.9950	1144.5070
11	1251.4030	1182.3440	1166.7310	1188.2880	1187.1860	1203.1510	1113.3650	1326.2540	1221.4000
12	1583.6870	1591.9170	1601.3440	1728.0000	1636.8240	1321.6180	1672.5210	1701.0010	1481.9390
13	702.5545	621.0868	691.8826	718.0733	689.1517	723.4783	943.0833	728.5265	845.5146
14	930.6376	901.0494	949.4356	947.4288	949.0155	964.4218	1016.8640	985.8364	1020.4140
15	1021.3630	1032.9920	1075.9460	1051.6730	1031.9230	1039.2100	891.2174	1055.3100	1107.0560
16	913.8994	894.4158	910.5151	910.8187	909.3431	926.7889	981.6817	990.9919	1037.8990
17	1331.0130	1420.8930	1348.0660	1335.1490	1297.6920	1276.7440	1356.6530	1732.7060	1721.6000
18	1348.6060	1409.0260	1610.0220	1308.5750	1358.3960	1350.0230	1355.0210	1490.9960	1525.7460
19	873.6953	866.5141	879.3327	864.7402	862.1920	751.6447	841.7512	893.9958	970.7055
20	696.5530	676.7407	731.2695	792.0228	717.7358	718.9481	873.7510	767.9837	795.8770
21	907.8507	880.3707	879.8113	889.6364	878.6407	896.9196	963.3410	779.9898	956.2853
22	1454.1070	1474.9710	1472.3880	1458.6950	1467.8850	1466.3370	1574.7330	1525.9980	1598.8590
23	1440.1470	1455.8440	1457.4890	1439.5860	1460.7250	1515.5380	1369.4030	1654.9970	1583.8190
24	1381.8480	1390.4390	1398.1390	1363.8520	1448.5090	1139.0030	1300.3410	1378.5470	1525.2910
25	1276.3700	1308.3720	1304.6120	1345.4210	1300.8230	1302.8890	939.7524	1402.9980	1260.4310
26	998.5577	949.3576	984.4049	940.4065	942.6237	937.9478	861.1636	998.9952	1049.4960
27	839.9656	815.5705	899.8967	853.6171	857.8741	859.9797	960.7563	828.7761	999.2051
28	1146.1890	1142.9240	1156.9800	1154.9740	1156.0930	1153.0060	1133.0360	1196.9990	1233.2610
29	1152.3870	1165.5970	1174.1420	1150.6750	1153.2870	1102.0590	1266.6250	1253.9960	1250.1170
30	1758.5260	1767.2630	2021.6820	1785.4070	1772.2720	1772.2720	1606.0670	1587.7610	1851.5880
31	1005.4010	1019.7920	1059.9820	981.6633	1009.1610	1022.9880	1125.9740	1086.6870	1101.3110
32	1148.2190	1134.7570	1147.3080	1138.0140	1146.9370	1154.1590	1274.3400	1240.9770	1222.6430
33	1352.2120	1334.9990	1379.0490	1359.4600	1373.4620	1364.0330	1863.9880	1477.0010	1308.9270
34	1696.3920	1818.7050	1343.2150	1779.6020	1550.3290	1772.3970	1551.4770	1980.9970	1835.5090
35	566.9703	491.8064	569.0225	561.4405	560.7351	592.8054	632.9525	599.5945	663.4965
36	1133.5810	1120.5190	1136.8210	1130.9230	1127.1200	1144.1670	1195.9900	1236.9960	1214.2140
37	1163.8940	1220.1170	1167.5240	1158.3880	1167.0830	1134.7290	1164.2550	1245.9970	1021.7730
38	1127.1180	1152.8300	1256.4520	1134.4680	1151.8300	1166.9300	1095.2060	1254.9930	1309.8180
39	1114.1670	1096.3070	1098.0490	1084.7650	1083.5040	1102.7260	1323.0720	1054.5340	1183.0110
40	1309.8380	1317.4720	1334.8050	1299.4060	1322.0240	1315.3580	1237.0530	1524.0010	1460.6390
41	641.2256	642.3794	634.3464	647.8603	633.3793	632.0134	733.9766	834.9984	760.2512
42	956.9164	892.8212	941.6143	940.4842	889.6043	953.8073	936.9060	1141.9930	1033.7160
43	1268.9700	1255.3170	1270.0200	1225.8510	1238.2740	1243.9630	1197.7730	1438.9980	1293.5380
44	981.0678	963.2432	983.9494	942.3786	972.1737	979.4640	898.6088	915.5674	1030.9460
45	1670.7840	1704.5120	1710.9470	1708.7000	1713.3280	1694.7600	1883.3770	1649.8680	1796.3070
46	1869.4200	1875.3520	1887.2350	1770.4470	1886.5030	1876.2370	1936.1090	1999.9100	1976.8690
47	906.2981	913.8651	972.1981	939.4036	941.4739	959.1903	1063.9870	986.0455	1034.6440
48	1168.2890	1277.1910	1167.5590	1162.5770	1167.4280	1171.6720	1326.9980	1267.9980	1238.4660
49	1324.6140	1328.6580	1328.7830	1322.4420	1334.1640	1330.1040	1348.2480	1527.9990	1388.9500
50	1176.9920	1190.9300	1172.6750	1145.7240	1170.4780	1176.8970	1171.9950	1371.9950	1201.9010

Table 6. Average Differences of the Results

Scheduling Policy	Neural Network Model	Average Difference, %
<b>FCFS</b>	<b>10 Hidden Node, L-M training Alg.</b>	<b>2,271795674</b>
FCFS	20 Hidden Node, L-M training Alg.	2,50928458
FCFS	30 Hidden Node, L-M training Alg.	11,31792847
FCFS	10 Hidden Node, C-G training Alg.	4,138162165
FCFS	20 Hidden Node, C-G training Alg.	5,204217314
FCFS	30 Hidden Node, C-G training Alg.	8,849168829
FCFS	10 Hidden Node, G-D training Alg.	2,437718382
FCFS	20 Hidden Node, G-D training Alg.	7,285583699
FCFS	30 Hidden Node, G-D training Alg.	7,410640241
LCFS	10 Hidden Node, L-M training Alg.	3,185375557
LCFS	20 Hidden Node, L-M training Alg.	3,211717432
LCFS	30 Hidden Node, L-M training Alg.	15,09407928
LCFS	10 Hidden Node, C-G training Alg.	3,07761742
LCFS	20 Hidden Node, C-G training Alg.	4,630245757
LCFS	30 Hidden Node, C-G training Alg.	5,167792174
<b>LCFS</b>	<b>10 Hidden Node, G-D training Alg.</b>	<b>2,982247861</b>
LCFS	20 Hidden Node, G-D training Alg.	4,114307727
LCFS	30 Hidden Node, G-D training Alg.	4,360410091
<b>SJF</b>	<b>10 Hidden Node, L-M training Alg.</b>	<b>2,028381072</b>
SJF	20 Hidden Node, L-M training Alg.	3,421056389
SJF	30 Hidden Node, L-M training Alg.	3,503745147
SJF	10 Hidden Node, C-G training Alg.	2,491615607
SJF	20 Hidden Node, C-G training Alg.	3,300253264
SJF	30 Hidden Node, C-G training Alg.	3,424767992
SJF	10 Hidden Node, G-D training Alg.	9,290039653
SJF	20 Hidden Node, G-D training Alg.	10,04691753
SJF	30 Hidden Node, G-D training Alg.	10,00751593