# Mixed Convection from Inclined Square Cylinder in a Square Cavity 

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#### Abstract

In this work, mixed convection from an inclined square cylinder in a cavity is numerically investigated. A commercial CFD solver Ansys Fluent is used to solve the problem. First, the inclined square cylinder is located at the center of the cavity, then the location of the cylinder is changed along the $x$-axis. The cavity walls are assumed to be adiabatic and the cylinder walls are assumed to be isothermal boundary condition. The Reynolds number, Re varies from 100 to 300 and the Grashof numbers, Gr range from $10^{3}$ to $10^{5}$ throughout the work. The working fluid is chosen as air at Prandtl number, $\operatorname{Pr}=0.7$. The Nusselt number, Nu variations, the distributions of velocity and isotherms are presented in Tables and Figures. The maximum Nusselt number, $N u$ is obtained as 11.47 at $\mathrm{Re}=300$ and $\mathrm{Gr}=10^{3}, 10^{4}$ when the cylinder location is at the right place of the cavity.


Keywords: cavity, flow structure, heat transfer, mixed convection.

# Kaviteye Yerleştirilen Açılı Kare Silindirden Doğal ve Zorlanmış Taşınım 


#### Abstract

Özet Bu çalışmada, kavite içerisine yerleştirilmiş bir açı verilmiş kare silindirde meydana gelen doğal ve zorlanmış taşınım araştırılmıştır. Çözüm için ticari bir yazılım olan Ansys Fluent program kullanılmışıır. Silindir ilk etapta kavite merkezine yerleştirilmiş, daha sonra ise kavite içerisinde $x$ ekseni boyunca farklı konumlarda bulundurulmuştur. Kavite duvarları yalıtımış, silindir duvarları ise belli bir sıcaklıkta tutulduğu kabul edilmiştir. Reynolds sayısı $100^{\prime}$ den $300^{\prime}$ e, Grashof sayısı ise $10^{3^{\prime}}$ den $10^{5^{\prime}}$ e kadar değişmektedir. Çalışma akışkanı olarak 0,7 Prandtl sayısındaki özelliklere sahip hava tercih edilmiştir. Nusselt sayısındaki değişim, hız ve sıcaklık izotermlerindeki dağılımlar şekiller ve tablolar vasıtasıyla sunulmuştur. Maximum Nusselt sayısı Re sayınının 300 ve Gr sayısının $10^{3}, 10^{4}$ değerlerinde, silindir konumunun kavitenin sağ kısmında bulunduğu durumda 11,47 olarak elde edilmiştir.


Anahtar kelimeler: akış yapısı, doğal ve zorlanmış taşınım, ısı transferi, kavite.

## 1. INTRODUCTION

The mixed convection from a square cylinder is mostly encountered in engineering applications such as cooling electronic equipment, solar collectors, etc. In this context, the topic of mixed convection from a hot cylinder placed in the square cavity attracts the attention of researchers. Chamkha et al. [1] conducted a numerical study to investigate the heat transfer and flow characteristics of a square cylinder placed in a square cavity. They implied different inlet/ outlet configurations to figure out the thermal characteristics. The Richardson number, Ri and Reynolds numbers, $R e$ varies from 0 to 10 and 50 to 200 , respectively. The results showed that the average Nusselt number, $N u$ of square cylinder upgrades as the Richardson and the Reynolds numbers rise. Mamun et al. [2] numerically investigated mixed convection in a square cavity in the presence of a hollow heated cylinder. The cavity was ventilated, while the walls of the cavity were adiabatic. Also, the cylinder diameter varied. They concluded that the maximum Nusselt number was obtained when the diameter of the cylinders was largest. Laidoudi [3] studied the heat transfer characteristics of two heated circular cylinders placed in a square enclosure. They claimed that the average Nusselt number, $N u$ increases with increasing Ri and Re numbers in the range of the study. Ali and Jalal [4] investigated natural convection from two heated circular cylinders placed in a square enclosure with different inlet and outlet ports. Both the locations of the cylinders and the inlet/outlet ports varied throughout the study, and it was seen that both of them were significant parameters that effect on the heat transfer rates. Mehrizi et al. [5] investigated mixed convection from an obstacle in a cavity in the case of the usage of nanofluid as a working fluid. The effect of the location of the inlet /outlet ports of the cavity was also examined. The Ri number varied from 0.1 to 10 and Grashof number, $G r$ was taken as $10^{4}$. Generally, using nanofluid as a working fluid increases the heat transfer rates; moreover, increasing the volume fraction of nanoparticles contributes to heat transfer. There are more works on hot bodies placed in a cavity [6-12].

Furthermore, researchers implied active and passive heat transfer enhancement techniques to upgrade convection in a vented cavity. Jasim et al. [13] conducted a numerical study by implying rotation to the cylinder placed in a vented cavity using a hybrid nanofluid as a working fluid. The diameter and location of the cylinder also were varied. Gr numbers range from $10^{3}$ to $10^{5}$ and Reynolds range from 50 to 500 . Their results showed that $21 \%$ heat transfer enhancement could be reached. Hamzah et al. [14] researched the mixed convection from a heated cylinder located near the two counter-rotating cylinders in a cavity. They calculated a maximum heat transfer enhancement of $20.9 \%$. Moayedi [15] investigated heat transfer from double-rotating cylinders in a cavity with different locations. Also, the variations of inlet and outlet ports were examined. The results showed that if the rotation direction is counterclockwise, a higher heat transfer rate was obtained than clockwise rotation. The average Nusselt number was enhanced as $56.03 \%$ with an optimum configuration. Additionally, magnetic field were also implied to improve heat transfer in cavities [16,21]. Time-varied flow at the inlet of the cavity was applied to enhance the heat transfer rates in the literature [22,23].

This study investigates mixed convection from an inclined square cylinder in a square cavity. The location of the inclined square cylinder varies along the x-axis. The effect of Grashof number, $G r$ and Reynolds numbers, $R e$ variations on the heat transfer and flow pattern is examined.

## 2. SYSTEM DESCRIPTIONS

### 2.2 Model Geometry



Figure 1. The schematic representations of the model
Figure 1 shows the schematic representations of the model geometry investigated. The center of the inclined square cylinder is located at the origin ( $\mathrm{x}_{0}, \mathrm{y}_{0}$ ) of the Cartesian coordinate system in the case of $\mathrm{L}_{0}=0$. Two other cases were examined, such as $\mathrm{L}_{0}=\mathrm{L} / 10$ and $\mathrm{L}_{0}=-\mathrm{L} / 10$. L represents the one-side length of the square cavity. The central axis of the inlet and outlet ports are symmetrical considering the center of the Cartesian coordinate system and their length, $h$ is taken as L/5. The walls of the cavity are assumed as adiabatic. The air as a working fluid enters the cavity from the inlet section uniformly at cold temperature, $T_{c}$. The inclined square cylinders are heated and their walls are kept at a hot temperature, $T_{h}$. The length of one side of the inclined square cylinder is taken as $\mathrm{L} / 2.5$. No-slip has implied all the walls of the cavity and inclined square cylinder.

### 2.2 Governing equations and solution procedure

In this work, the flow is assumed as laminar, two-dimensional, incompressible and at a steady state. Pr number is taken as 0.7 . The thermophysical properties of the working fluid are constant, except the density. Boussinesq approximation was applied to the density of the working fluid. In addition, radiation and viscous dissipation are insignificant. The governing equations are as follows,

Continuity equation,
$\frac{\partial u}{\partial x}+\frac{\partial v}{\partial x}=0$
Momentum equations,
$u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}=-\frac{1}{\rho} \frac{\partial p}{\partial x}+\frac{\mu}{\rho}\left(\frac{\partial^{2} u}{\partial x^{2}}+\frac{\partial^{2} u}{\partial y^{2}}\right)$
$u \frac{\partial v}{\partial x}+v \frac{\partial v}{\partial y}=-\frac{1}{\rho} \frac{\partial p}{\partial x}+\frac{\mu}{\rho}\left(\frac{\partial^{2} v}{\partial x^{2}}+\frac{\partial^{2} v}{\partial y^{2}}\right)+\beta g\left(T-T_{c}\right)$
Energy equation,
$\left(u \frac{\partial T}{\partial x}+v \frac{\partial T}{\partial y}\right)=a\left(\frac{\partial^{2} T}{\partial x^{2}}+\frac{\partial^{2} T}{\partial y^{2}}\right)$
where $a=k / \rho c_{p}{ }^{\prime}$ dir.
The dimensionless parameters are as follows,
$\mathrm{X}=\mathrm{x} / \mathrm{L}, \mathrm{Y}=\mathrm{y} / \mathrm{L}, \theta=\frac{T-T_{c}}{T_{h}-T_{c}}, R e=\frac{u_{i} L}{\vartheta}, G r=\frac{g \beta\left(T_{h}-T_{c}\right) L^{3}}{\vartheta^{2}}, \mathrm{Pr}=\vartheta / a$
The local Nusselt number, $N u_{y}$ can be calculated as follows,
$N u_{y}=-\left(\frac{\partial \theta}{\partial Y}\right)_{Y=0}$
The average Nusselt number, $N u_{\text {avg }}$ can be calculated as follows,
$N u_{\text {avg }}=\frac{1}{L} \int_{X=0}^{X=L} N u_{y} d X$
The boundary conditions at the inlet are $\mathrm{U}=1, \mathrm{~V}=0$ and $\theta=0$
The boundary conditions at the outlet are $\frac{\partial U}{\partial X}=0, \frac{\partial V}{\partial X}=0$ and $\frac{\partial \theta}{\partial X}=0$ and $\mathrm{P}=0$
The boundary conditions at the cavity wall are $\mathrm{U}=0, \mathrm{~V}=0$ and $\frac{\partial \theta}{\partial X}=0$
The boundary conditions for an inclined square cylinder are $\mathrm{U}=0, \mathrm{~V}=0$ and $\theta=1$
A commercial CFD solver Ansys Fluent [24] is used to solve the problem. The finite volume technique was applied. A simple algorithm was selected. Second order upwind technique was used to discretized equations 1-4. Consequently, iterations were carried on until convergence criteria $1 \times 10^{-8}$ were reached.

The mesh used in the study and the element type is illustrated in Fig. 2. In this figure, 20372 triangular elements with 11506 nodes are used. The mesh type and nodes are acceptable and verify the accuracy. Furthermore, a validation study was conducted. It was noted that the current study results agreed with the results by Lee et al. [25], who performed an analysis to investigate the convection from a heated circular cylinder in a cavity. The hot cylinder was located in a square enclosure in their study. The walls were in isothermal conditions. In the validation case, Rayleigh's number was taken as $10^{5}$. They found the mean Nusselt number as 7.76 . When the same boundary conditions were applied in the current study, the mean Nusselt number was obtained as 7.86 with a $1 \%$ difference.


Figure 2. The triangular mesh distribution

## 3. RESULTS AND DISCUSSION

Table 1 indicates the Nusselt number, Nu variation with increasing Reynolds number, Re at $\mathrm{Gr}=10^{3}$. As seen, the Nusselt number is sensitive to the displacement of the inclined square cylinder in the cavity. The Nusselt number first decreases then increase as the body moves from left to right for all Reynolds numbers, $R e . \mathrm{L}_{0}=\mathrm{L} / 10$ and $\mathrm{L} 0=-\mathrm{L} / 10$ represent the right and left positions of the cylinders in the cavity, respectively. It is noted that the Nu number is higher in the case of $\mathrm{L}_{0}=\mathrm{L} / 10$ than in the case of $\mathrm{L}_{0}=$ $\mathrm{L} / 10$. The highest heat transfer rate is taken place in the case of $\mathrm{L}_{0}=-\mathrm{L} / 10$ at the Reynolds number of 300. As can be seen, the heat transfer upgrades with increasing Reynolds numbers. The effect of the increment Grashof number, $G r$ is evaluated in Tables 2 and 3. While any significant changes are taken place in the case of $\mathrm{Gr}=10^{4}$, the deterioration of heat transfer rates from the cylinders in the cavity stands out in the case of $\mathrm{Gr}=10^{5}$. At the Reynolds number of 100 and the location of $\mathrm{L}_{0}=0$, the deterioration reaches $28 \%$ in the case of $\mathrm{Gr}=10^{5}$ compared to the case of $\mathrm{Gr}=10^{4}$. The lowest Nusselt number, Nu is obtained as 4.66 for $\mathrm{Re}=100$ at the cylinder's position of $\mathrm{L}_{0}=0$. When the Reynolds number increases, the forced flow dominates flow structures in the cavity and consequently, the heat transfer rates upgrades. With this context, the increase rate attains $129 \%$ from $80 \%$ in the case of $\mathrm{L}_{0}=\mathrm{L} / 10$ when the Grashof number increases from $\mathrm{Gr}=10^{3}$ to $\mathrm{Gr}=10^{5}$.

Table 1. Nu number, Nu variation with increasing Re number $\left(\mathrm{Gr}=10^{3}\right)$

| Re | $\mathrm{Nu}\left(\mathrm{L}_{0}=-\mathrm{L} / 10\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=0\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=\mathrm{L} / 10\right)$ |
| :---: | :---: | :---: | :---: |
| 100 | 6.32 | 6.16 | 6.37 |
| 200 | 9.16 | 8.97 | 9.43 |
| 300 | 11.06 | 10.79 | 11.47 |

Table 2. Nu number, $N u$ variation with increasing Re number $\left(\mathrm{Gr}=10^{4}\right)$

| Re | $\mathrm{Nu}\left(\mathrm{L}_{0}=-\mathrm{L} / 10\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=0\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=\mathrm{L} / 10\right)$ |
| :---: | :---: | :---: | :---: |
| 100 | 6.32 | 6.09 | 6.29 |
| 200 | 9.17 | 8.96 | 9.42 |
| 300 | 11.06 | 10.79 | 11.47 |

Table 3. Nu number, Nu variation with increasing Re number $\left(\mathrm{Gr}=10^{5}\right)$

| Re | $\mathrm{Nu}\left(\mathrm{L}_{0}=-\mathrm{L} / 10\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=0\right)$ | $\mathrm{Nu}\left(\mathrm{L}_{0}=\mathrm{L} / 10\right)$ |
| :---: | :---: | :---: | :---: |
| 100 | 5.72 | 4.66 | 4.79 |
| 200 | 9.19 | 8.11 | 8.63 |
| 300 | 11.14 | 10.68 | 11.34 |



Figure 3. Velocity distributions for different configurations at $\mathrm{Gr}=10^{3}$
The distribution of velocity in the cavity with the presence of the inclined square cylinder is seen in Figure 3 for different locations of the body at $\mathrm{Gr}=10^{3}$. The magnitudes of the $\left\langle\mathrm{V} / \mathrm{V}_{\text {in }}\right\rangle$ can be followed by the legend at the top. When the dark blue contours represent the minimum values, the dark red represents the maximum values. The symmetry concerning the center of the cylinder in the flow pattern is seen. The flow splits when it enters the cavity from the inlet port. The bifurcated fluid follows almost the same trajectory at both sides of the inclined square cylinder and exits from the outlet port of the cavity. Besides, recirculation regions near the upper and lower corners of the cavity are formed when the fluid enters the cavity. The recirculation regions enlarge in size and the severity increases when the Reynolds numbers rise in all cases. Moreover, additional recirculating regions are taken place on the right sides of the cylinder in the cavity when the Reynolds number reaches the value of 300 . The aforementioned regions occupy more area when the inclined square cylinders move from left to right.


Figure 4. Velocity distributions for different configurations at $\mathrm{Gr}=10^{4}$
The effect of the increase in the number of Grashof numbers, $G r$ has begun to be seen in Figure 4, especially for low Reynolds numbers. Some incoming flow is forced to the bottom side of the inclined square cylinders compared to the upper sides of the cavity at the Reynolds number of 100. However, the forced convection becomes dominant as Reynolds number increases. Namely, the symmetrical velocity distribution is taken place. The recirculating regions still exist in vicinity of the right sides of the cylinder in the cavity when the Reynolds number reaches the value of 300 . It is notes they are the symmetrical concerning the center of the square cavity. These recirculating regions shrink in size when the inclined square cylinders move from left to right location of the cavity.


Figure 5. Velocity distributions for different configurations at $\mathrm{Gr}=10^{5}$
The bouncy force becomes dominant at a lower Reynolds number, as seen in Figure 5. The recirculation region near the upper sides of the cavity forces the fluid to flow to the bottom side of the cavity. Almost all the fluid flows throughout the bottom side since the fluid is trapped at the upper region resulting higher pressure. Hence, the heat transfer from the top side of the inclined square cylinder decreases. It is noted there is another recirculating region near the outlet port at the upper side of the cavity. Due to the bouncy forces, a small recirculation is situated in the vicinity of the bottom side of the cylinder. On the other hand, the symmetry that was present in previous Gr numbers at Reynolds number of 300 is disappear in this case. The recirculating region near the entrance at the upper side of the cavity enlarges when the body moves from left to right. However, as the momentum of the fluid increases, fluid flows in the vicinity of the upper side of the cylinder, especially at the Reynolds number of 300. The recirculating regions taken place in the cavity are forced to shrink in size by the main flow region.


Figure 6. The distribution of isotherms for different configurations at $\mathrm{Gr}=10^{3}$
Figure 6 depicts the distribution of isotherms for the inclined square cylinder in the cavity at $\mathrm{Gr}=10^{3}$. The distribution of the isotherms is symmetrical concerning the center of the cylinder in all cases. The thermal boundary layer is thinner on the left side than on the right side due to the fluid with high momentum at the front side of the cylinder. Additionally, the thermal boundary layer becomes thinner as the Reynolds number increases. The cylinder locations are essential in terms of the temperature distribution of the cavity. This occasion is also valid for the Reynolds number increments. When the Reynolds number increases, the isotherms with high values occupies lower region comparatively in the cavity.


Figure 7. the distribution of isotherms for different configurations at $\mathrm{Gr}=10^{4}$
Figure 7 reveals the contour of the isotherms in the cavity at $\mathrm{Gr}=10^{4}$. The effect of the Grashof number, Gr emanates especially for low Reynolds numbers. The symmetrical distribution of isotherms is dissipated in the cavity. With an increase in the Reynolds number, the symmetrical distribution is restored. Figure 8 depicts the patterns of the isotherms in the cavity at $\mathrm{Gr}=10^{5}$. The asymmetry is clearly seen from the contours of the temperature in the cavity at the Reynolds number of 100. Since the fluid is trapped at the upper sides of the cavity, the heat transfer rates deteriorate in this case. However, the heat transfer rates increase as the flow momentum increases with a higher Reynolds number, Re. The thermal boundary layer gets thinner as flow momentum rises.


Figure 8. The distribution of isotherms for different configurations at $\mathrm{Gr}=10^{5}$

## 4. CONCLUSION

The heat transfer characteristics and flow structures are evaluated to investigate the mixed convection from an inclined square cylinder in a cavity. A commercial CFD solver Ansys Fluent is utilized to perform the analysis. The results showed that while the bouncy forces considerably affect the flow structures at low Reynolds numbers, forced convection becomes dominant when the Reynolds number increases. Reynolds number is an important parameter that affects the heat transfer rates remarkably. For example, when the Reynolds number increases from 100 to 300, the heat transfer rate attains $129 \%$ in the case of $\mathrm{Gr}=10^{5}$. While the maximum average Nusselt number, $N u$ is obtained as 11.47 for the case of $\mathrm{L}_{0}=\mathrm{L} / 10$, the minimum average Nusselt number is obtained as 4.66 for the case of $\mathrm{L}_{0}=0$. In addition, the inclined square cylinder's location in a cavity considerably affects the flow patterns. For instance, the Nusselt number is 5.72 in the case of $\mathrm{L}_{0}=-\mathrm{L} / 10$. However, it declines about $18 \%$ and becomes 4.66 in the case of $\mathrm{L}_{0}=0$ at $\mathrm{Re}=100$ and $\mathrm{Gr}=10^{5}$.

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